

Writing arguments using the Fitch bar:

1		P_1	
2		P_2	Premises
3		:	
4		C	Conclusion

For example:

1		Socrates is a man	
2		All men are mortal	
3		Socrates is mortal	

Writing proofs using the Fitch bar:

1		P_1	
2		P_2	Premises
3		\vdots	
<hr/>			
4		S_1	
5		S_2	Steps
6		\vdots	
7		C	Conclusion

If each step is valid, argument from premises to conclusion will be valid. Proof by contradiction: If the premises are true, what is the first line that could be false?

Introducing Reiteration (Reit):

n		P	
		\vdots	
\triangleright		P	R, n

Informal Example:

1		Snow is white.	
		<hr/>	
2		Snow is white.	R, 1

Formal (FOL) Example:

1		$Large(a)$	
2		$Small(b)$	
		<hr/>	
3		$Small(b)$	R, 1

Formal statement of equality introduction:

$$\triangleright \left| a = a \quad =\text{Intro} \right.$$

Formal statement of equality elimination:

$$\begin{array}{l} n \\ \vdots \\ m \\ \vdots \\ \triangleright \end{array} \left| \begin{array}{l} c = d \\ \\ P(c) \\ \\ P(d) \end{array} \right. =\text{Elim, } n, m$$

Ana Con, Taut Con, FO Con

There are no simple rules that involve the block language predicates, must use Ana Con instead. For example:

$$\begin{array}{l|l} 1 & \textit{FrontOf}(a, b) \\ 2 & \textit{FrontOf}(b, c) \\ \hline 3 & \textit{FrontOf}(a, c) \quad \text{AnaCon, 1, 2} \end{array}$$

AnaCon is extremely powerful, so often homework instructions will put constraints on your usage of it.

Nonconsequence

Rules of thumb:

- To show an argument is valid: exhibit proof
- To show an argument is *invalid*: exhibit counterexample

This makes sense if we look at the definition of validity.

- To prove an argument valid we must show the absence of a certain type of possibility.
- To prove an argument invalid we only need to show the existence of a certain type of possibility.

You might expect that it would be easier to refute an argument in FOL than to prove it. Remarkable fact: opposite is true!